Math 026L.04 Spring 2002 January 23, 2002

## 1. Page 50 #35

The depth of water in a tank oscillates sinusoidally once every 6 hours. If the smallest depth is 5.5 feet and the largest depth is 8.5 feet, find a possible formula for the depth in terms of time in hours.

# 2. Page 51 #39

- (a) Use a graphing calculator or computer to estimate the period of  $2\sin(\theta) + 3\cos(2\theta)$ .
- (b) Explain your answer, given that the period of  $\sin(\theta)$  is  $2\pi$  and the period of  $\cos(2\theta)$  is  $\pi$ .

#### **3.** Page 161 #73

The depth of water, y, in meters, in the Bay of Fundy is given as a function of time, t, in hours after midnight, by the function

$$y = 10 + 7.5\cos(0.507t).$$

How quickly is the tide rising or falling (in m/h) at each of the following times?

- (a) 6:00 am
- (b) 9:00 am
- (c) Noon
- (d) 6:00 pm

## 4. Page 159 #65

The graphs of  $\sin x$  and  $\cos x$  intersect once between 0 and  $\pi/2$ . What is the angle between the two curves at the point where they intersect? (You need to think about how the angle between two curves should be defined.)

#### 5. Page 159 #57

Assuming y is a differentiable function of x, find  $\frac{dy}{dx}$  if

$$\sin(ay) + \cos(bx) = xy.$$

- 6. For each part below, compute the derivative of the given function.
- (a) Page 159 #6

$$z = \sin^3 \theta$$

(b) Page 159 #14

$$s(x) = \arctan(2 - x)$$