Math 103.01 Summer 2000 June 12, 2001

1. Use a triple integral to find the volume of the tetrahedron T bounded by the planes x + 2y + z = 2, x = 2y, x = 0, and z = 0.

2. Express the integral

$$\int \int \int_T f(x, y, z) dV$$

as an iterated integral in six different ways, where T is the solid bounded by the given surfaces:

a.
$$z = 0, x = 0, y = 2, z = y - 2x$$

b.
$$9x^2 + 4y^2 + z^2 = 1$$

3. Evaluate

$$\int \int \int_T \sqrt{x^2 + z^2} \, dV$$

where T is the region bounded by the paraboloid $y = x^2 + z^2$ and the plane y = 4.

4. Evaluate

$$\int \int \int_T x + 2y \ dV$$

where T is the region bounded by the parabolic cylinder $y = x^2$ and the planes x = z, x = y, and z = 0.