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# Development of an artificial neural network model for predicting minimum miscibility pressure in CO<sub>2</sub> flooding

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## Abstract

This paper presents the development of an artificial neural network (ANN) model for the prediction of pure and impure CO<sub>2</sub> minimum miscibility pressures (MMP) of oils. The pure CO<sub>2</sub> MMP of a reservoir fluid (live oil) is correlated with the molecular weight of C<sub>5+</sub> fraction, reservoir temperature, and concentrations of volatile (methane) and intermediate (C<sub>2</sub>–C<sub>4</sub>) fractions in the oil. The impure CO<sub>2</sub> MMP factor,  $F_{imp}$ , is predicted by correlating the concentration of contaminants (N<sub>2</sub>, C<sub>1</sub>, H<sub>2</sub>S and SO<sub>2</sub>) in CO<sub>2</sub> stream and their critical temperatures. The  $F_{imp}$  is a correction factor to the MMP of pure CO<sub>2</sub>. The advantage of using the ANN model is evaluated by comparing the measured MMP values with the predicted results from the ANN models as well as those from other statistical methods. The developed ANN models are able to reflect the impacts on CO<sub>2</sub> MMP of molecular weight of C<sub>5+</sub> fraction, reservoir temperature, and solution gas in the oil. The ANN model of impure CO<sub>2</sub> MMP factor can distinguish the effects on MMP of different contaminants in the CO<sub>2</sub> stream. It can also be used to predict the CO<sub>2</sub> MMP of a reservoir oil and the level of contaminants in the CO<sub>2</sub> stream which can be tolerated for a miscible injection.

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**Keywords:** Artificial neural network; Minimum miscibility pressure; CO<sub>2</sub> flooding

## 1. Introduction

Over the last two decades, carbon dioxide injection has become the leading enhanced oil recovery (EOR) process for light oils (Grigg and Schechter, 1997). The CO<sub>2</sub> injection can prolong, by 15 to 20 years, the production life of light oil fields nearing depletion under waterflood; the method could recover 15% to

25% of the original oil in place. It also brings environmental benefits by facilitating storage of CO<sub>2</sub> in the reservoir.

In a miscible CO<sub>2</sub> flood, multiple-contact miscibility between the injected CO<sub>2</sub> and the reservoir fluid can be achieved at pressures greater than a minimum value that is referred to as minimum miscibility pressure (MMP). The MMP is the single most important parameter in designing a miscible flood. It has been recognized that the MMP for CO<sub>2</sub> in a reservoir depends on oil temperature, oil composition, and CO<sub>2</sub> purity. The latter parameter is the only one that operators can influence. Some contaminants, mainly

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45 N<sub>2</sub> in the flue gas and CH<sub>4</sub> from the reservoir-  
46 produced gas, in CO<sub>2</sub> can either increase or reduce  
47 the CO<sub>2</sub> MMP. Since separation of CO<sub>2</sub> could be  
48 costly, reinjecting recycled CO<sub>2</sub> without removing  
49 hydrocarbon gases could make the process more  
50 attractive economically. Therefore, for a reservoir,  
51 the CO<sub>2</sub> MMP and the tolerable level of contaminants  
52 in the CO<sub>2</sub> stream are key parameters for design of a  
53 miscible CO<sub>2</sub> flood system, as well as the associated  
54 gas separation and field injection components.

55 Numerous empirically derived and thermodynamic  
56 models for predicting CO<sub>2</sub> MMP have been reported  
57 in the literature. Enick et al. (1988) provided a review  
58 of the related literature. Some of the empirical corre-  
59 lations disregarded the C<sub>1</sub> through C<sub>4</sub> fraction and  
60 were based only on the reservoir temperature and the  
61 molar weight of C<sub>5+</sub> fraction in the oil. Alston et al.  
62 (1985) offered an empirical correlation that accounts  
63 for the effect on MMP caused by solution gas present  
64 in reservoir fluids. The minimum miscibility pressure  
65 was correlated with reservoir temperature, the oil's C<sub>5+</sub>  
66 molecular weight, volatile oil fraction (CH<sub>4</sub>+N<sub>2</sub>),  
67 intermediate oil fraction (C<sub>2</sub> to C<sub>4</sub>, H<sub>2</sub>S, and CO<sub>2</sub>),  
68 and composition of the CO<sub>2</sub> stream. More recently,  
69 Zuo et al. (1993) modified the correlation derived by  
70 Johnson and Pollin (1981) by introducing two composi-  
71 tional parameters: the mole fractions of the light and  
72 the intermediate components in reservoir fluids.  
73 Although these two correlations account for the effect  
74 on MMP of solution gas, it was found (Dong et al.,  
75 2000) that they could not provide satisfactory predic-  
76 tion of MMP for reservoir oils that had high solution-  
77 gas-to-oil ratios and high volatile-component fractions.  
78 It was realized (Dong et al., 2000) that, to improve the  
79 MMP prediction accuracy, the effects of solution gas in  
80 CO<sub>2</sub> (and thus the amounts of volatile and intermediate  
81 fractions in oil) should be considered.

82 Among the empirical models, only those of Alston  
83 et al. (1985) and Sebastian et al. (1985) took into  
84 account the effects on CO<sub>2</sub> MMP of contaminants in  
85 the CO<sub>2</sub> stream. Results of the two models were  
86 tested, with the outcomes indicating that the effects  
87 of impurities on CO<sub>2</sub> MMP were not effectively  
88 reflected.

89 The development of statistical models for CO<sub>2</sub>  
90 MMP prediction has been a subject that involved  
91 extensive research efforts, resulting in many publica-  
92 tions (Dunyushkin and Namiot, 1979; Cronquist,

1978; Yellig and Metcalfe, 1980; Mungan, 1981; 93  
Sebastian et al., 1984; Alston et al., 1985; Kovarik, 94  
1985). However, the main concern with statistical 95  
techniques is the difficulties in satisfying many rigid 96  
assumptions that are essential for justifying their 97  
applications, such as those of sample size, linearity, 98  
and continuity. One alternative approach for system 99  
forecasting is the technique of artificial neural net- 100  
work (ANN) based on the theory of artificial intelli- 101  
gence. The massive interconnections in the ANN 102  
framework produces a large number of degrees of 103  
freedom, or fitting parameters, and thus may allow it 104  
to reflect the system's complexity more effectively 105  
than conventional statistical techniques. Recently, 106  
methods of artificial neural networks have been 107  
applied to petroleum engineering in a number of areas 108  
such as well-test analysis, well-log interpretation, 109  
reservoir characterization, and more recently, PVT 110  
and permeability studies for crude oils (Waller and 111  
Rowell, 1994; Gharbi and Elsharkawy, 1996, 1999). 112

113 This study is an extension of the previous efforts,  
114 emphasizing on the development of an ANN model  
115 for predicting CO<sub>2</sub> MMP. The main purpose is to  
116 examine the effects of (a) solution gas in CO<sub>2</sub>, (b)  
117 amount of volatile and intermediate fractions in oil,  
118 and (c) their ratio on pure CO<sub>2</sub> MMP, through the  
119 developed ANN model. Firstly, the interrelations of  
120 pure CO<sub>2</sub> MMPs (of live oils) with (a) molecular  
121 weight of C<sub>5+</sub> fraction, (b) reservoir temperature, (c)  
122 volatile oil fraction (methane and nitrogen gas), and  
123 (d) intermediate oil fraction (C<sub>2</sub>–C<sub>4</sub> and CO<sub>2</sub>, H<sub>2</sub>S)  
124 will be analyzed, resulting in a trained ANN model;  
125 the trained model will then be used to predict CO<sub>2</sub>  
126 MMP, with the results being compared with the  
127 measured live oil MMP values reported in the liter-  
128 ature. Secondly, the correlations between the impure  
129 CO<sub>2</sub> MMP factor ( $F_{imp}$ ) and the contaminant concen-  
130 trations (for N<sub>2</sub>, C1, H<sub>2</sub>S, and SO<sub>2</sub>) in the CO<sub>2</sub> stream  
131 will be examined. The  $F_{imp}$  represents the effect on  
132 CO<sub>2</sub> MMP of contaminants in CO<sub>2</sub> stream. Lastly, the  
133 developed ANN models will be used to predict the  
134 variations of CO<sub>2</sub> MMP with MW of C<sub>5+</sub> fraction,  
135 temperature of reservoir, and contaminant contents in  
136 CO<sub>2</sub> stream. In addition, the effectiveness of the  
137 developed ANN models will be evaluated by compar-  
138 ing the prediction results with (a) the measured MMP  
139 levels and (b) the prediction results from other stat-  
140 istical models.

ANN's main difference from statistical methods is its relinquishment in terms of strict conditions for data samples and associated assumptions. This is applicable to the existing situation of data availability for impure CO<sub>2</sub> MMP factors, which is not good enough for either statistical or numerical modeling. At the same time, analytical models are advantageous over the ANN in terms of its touching the detailed mechanisms of interactions among various impact factors; at the same time, such methods' limitations are also from their attempts to specify the complicated processes by detailed mathematical formulations, since many uncertain, interactive, and dynamic system components can hardly be expressed as accurate analytical formulations. Under such a situation, ANN becomes the only usable tool for analyzing the related effects and interactions; it can be used without violating either a number of prerequisites associated with statistical models or being forced to assuming unrealistic or over-simplified system conditions that are needed for analytical simulation.

## 2. Model development

In biology, a neural network is an array of neurons in the brain that processes information from input stimuli to produce comprehensible sensations. In the computer world, a neural network is a computer architecture that resembles its operators' process numerical inputs to generate outputs that are in some way meaningful to the user. Artificial neural networks (ANNs) are characterized as computational models with particular abilities to adapt, learn, generalize, recognize, cluster, and organize data (Dayhoff, 1990). ANNs are computing tools composed of many simple interconnected elements called neurons by analogy with neurophysiology. ANNs have a unique ability of recognizing underlying relationships between input and output events. They are well suited for modeling systems with complex relationships among incomplete or noisy data sets. Petroleum engineering applications of ANNs include areas such as well-test analysis, well-log interpretation, field development, reservoir characterization, formation damage, production, and drilling.

A typical neuron is shown in Fig. 1. A neuron has two components (Dayhoff, 1990): (1) a weighted

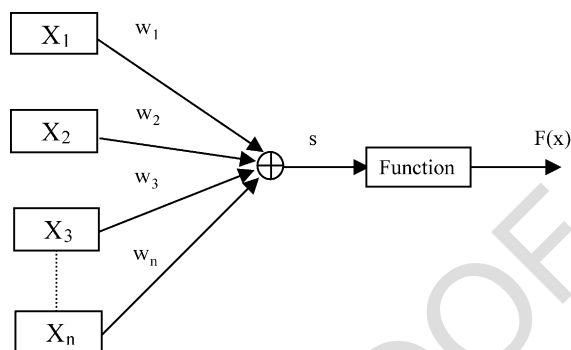


Fig. 1. Basic components of a neuron.

summer which perform a weighted summation of its inputs with components ( $X_1, X_2, X_3, \dots, X_n$ ), i.e.,  $s = \sum w_i X_i + b$ , where  $b$  is the bias of the networks; and (2) a linear, nonlinear or logic function which gives an output corresponding to  $s$ . Here, many kinds of functions can be used, including threshold (logic), sigmoid, hyperbolic tangent and Gaussian functions. In this study, each of them is examined at each neuron during the training process in order to get desired ANNs. In a typical ANN, there are three types of neurons: input neurons which may receive external data, output neurons which send data out of the ANN, and hidden neurons whose signals remain within the ANN. There are three types of layers corresponding to the types of neurons. The hidden neurons may form one or more hidden layers. The neurons in each layer are usually fully interconnected with neurons from neighboring layers. The importance of each inter-neuron connection is determined by its numerical value. A three-layered back-propagation network structure is depicted in Fig. 2 (Dayhoff, 1990). The ANN shown in Fig. 2 has an input layer, an output layer, and one hidden layer. The input layer contains an array of variables into which the input data of the system are read from an external source. Similarly, the predicted data or results, which can be multiple vectors, are written in the output layer. Initially, the input layer receives the input and passes it to the hidden layer. If more hidden layers exist, the processed information from the first hidden layer is then passed the next hidden layer for processing. Finally, the output layer receives information from the last hidden layers. In this study, the number of hidden layer is not fixed. The training tool will automatically

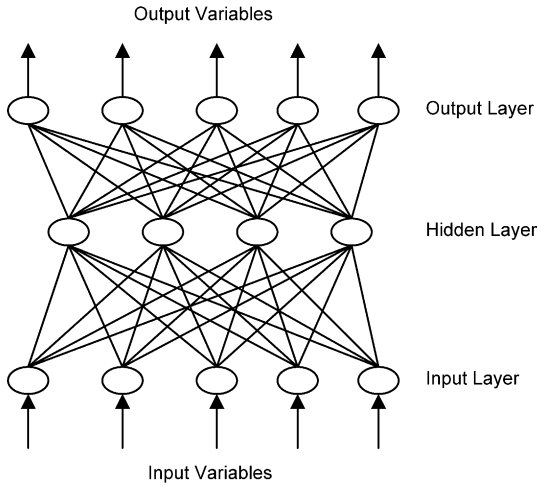


Fig. 2. A fully interconnected three-layered back-propagation network.

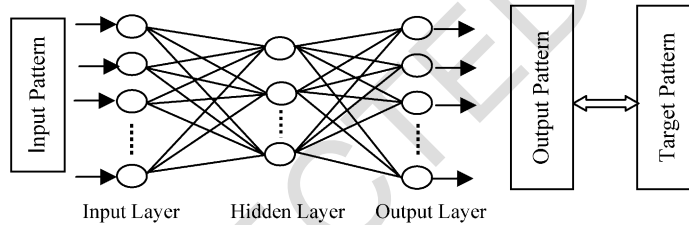
select suitable number of hidden layer to get the desired ANN model.

When an ANN is constructed, small numbers (weights) are assigned randomly to the connections between neurons. In general, the output from neural  $j$  in layer  $k$  can be calculated by the following equation:

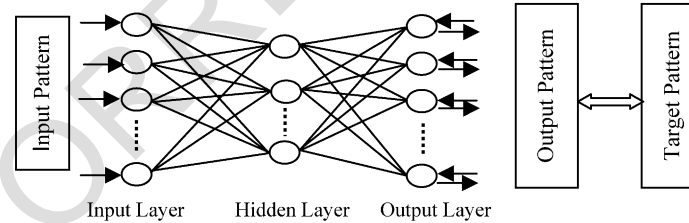
$$u_{jk} = F_k \left( \sum_{i=1}^{N_{k-1}} w_{ijk} u_{i(k-1)} + b_{jk} \right)$$

Coefficients  $w_{ijk}$  and  $b_{jk}$  are connection weight and bias of the network, respectively; they are fitting parameters of the model. The purpose is to obtain a mapping from an input vector to an output one. It is desired that the difference between the predicted and the observed (actual) values in the output vector be as small as possible. The fitting parameters are modified

(a) Output pattern is calculated, and then compared with target pattern:



(b) Errors are calculated for the output layer, and then incoming weights are adjusted (The arrows represent flows of information):



(c) Errors are calculated for the hidden layer, and then the incoming weights are adjusted (Heavy lines indicate that the errors are communicated from the output layer):

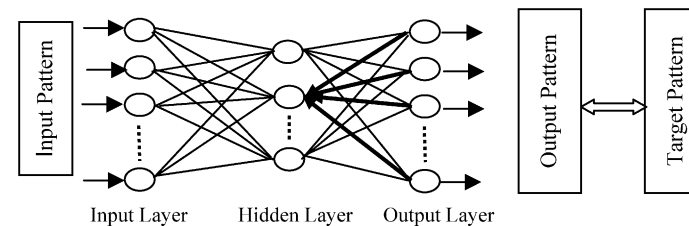


Fig. 3. Basic back-propagation dynamics.

235 until an error criterion between the input and the output  
 236 is satisfied based on the topology of the ANN and the  
 237 learning technique. The adjustment of the weights is  
 238 defined as the learning process. The ANN is tested  
 239 with input/output values used in training. After train-  
 240 ing and testing, the network is ready to perform tasks  
 241 such as pattern recognition, classification, or function  
 242 approximation. There are mainly two types of net-  
 243 works, feed-forward networks and recurrent networks.  
 244 In this study, the back-propagation technique with  
 245 momentum is used. The fitting procedure from which  
 246 weights  $w_{ijk}$  are determined is performed using a least-  
 247 squares minimization routine. In this routine, the sum  
 248 of root-squared relative errors between the calculated  
 249 and the experimental data is to be minimized. In  
 250 general, the back-propagation method uses the follow-  
 251 ing steps (Fig. 3):

- 252 (a) Read a specific input and calculate its correspond-  
 253 ing output.  
 254 (b) If the error between the produced output and the  
 255 desired output is acceptable, then stop.  
 256 (c) If the error is unacceptable in step (b), then the  
 257 weights are adjusted for all of the interconnections  
 258 that go into the output layer. Next, an error value  
 259 is calculated for all of the units in the hidden layer  
 260 that is just below the output layer. Then, the  
 261 weights are adjusted for all interconnections that

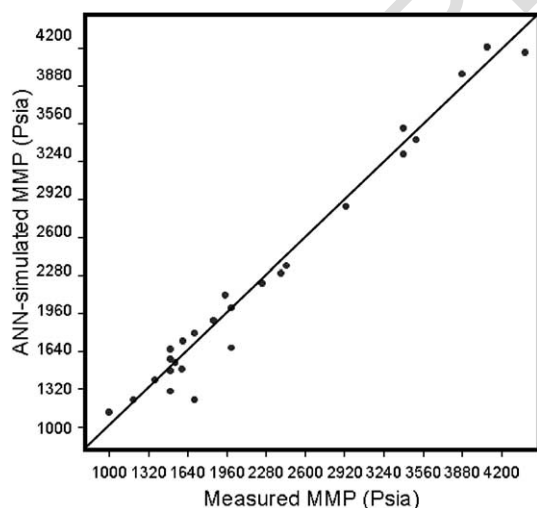


Fig. 4. The measured versus ANN-simulated MMP values (with °F for temperature).

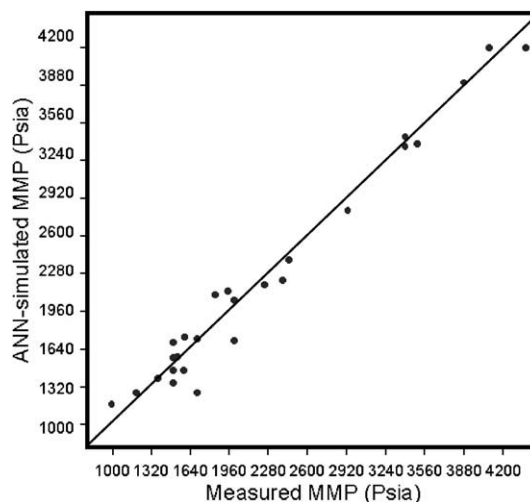


Fig. 5. The measured versus ANN-simulated MMP values (with K for temperature).

go into the hidden layer. The process is continued  
 until the last layer of weights has been adjusted.

Typically, an application of back-propagation  
 requires both a training set and a test set. Both  
 the two sets contain input/output pattern pairs.  
 While the training set is used to train the net-  
 work, the test set is used to assess the perfor-  
 mance of the network after the training is com-  
 plete. To provide the best test of network per-  
 formance, the test set should be different from  
 the training set. The most successful ANN archi-  
 tecture is the one that has the smallest predic-  
 tion error on a data set for which it was not  
 trained. For pure CO<sub>2</sub> MMP modeling, the reser-  
 voir temperature  $T$ , molecular weight of C<sub>5+</sub>,  
 volatile oil fraction  $X_{vol}$ , and intermediate oil  
 fraction  $X_{int}$  are selected as input variables.  
 Minimum miscibility pressure (MMP) is the  
 output variable. The data used for developing  
 the ANN model are from Jacobson (1972),  
 Dicharry et al. (1973), Wittstrom and Hage-  
 meier (1978), White and Lindsay (1972),  
 Graue and Zana (1981), Gardner et al. (1981),  
 Frimodig et al. (1983), Cardenas et al. (1984),  
 and Alston et al. (1985). Two scenarios of  
 reservoir temperature are used: one with the  
 degree Fahrenheit (°F) (Alston et al., 1985)  
 and the other with the Kelvin (K).

For modeling the impure CO<sub>2</sub> MMP factor ( $F_{imp}$ ),  
 the concentrations of different components in the gas



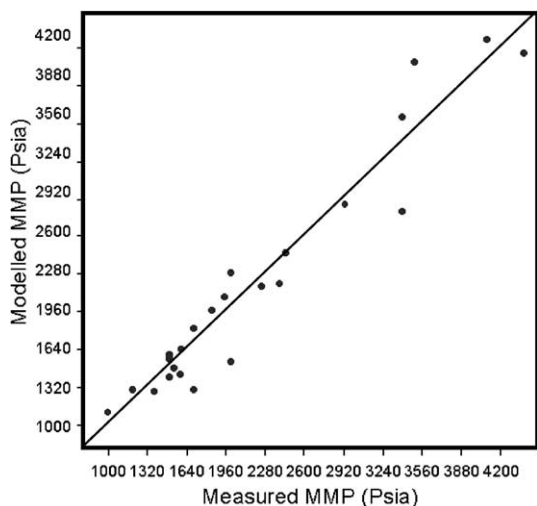


Fig. 6. The measured versus modeled MMP values (from Alston et al., 1985).

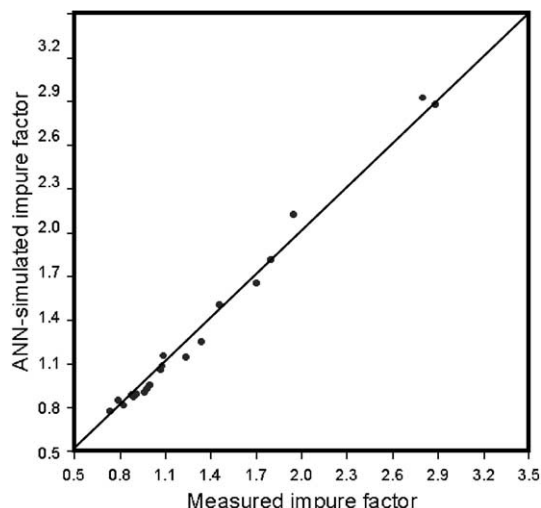


Fig. 7. The measured versus ANN-simulated impure factors.

290 mixture (CO<sub>2</sub> and contaminants) are used as input  
 291 variables. Based on data availability and importance  
 292 of the contaminants, N<sub>2</sub>, CH<sub>4</sub>, H<sub>2</sub>S, and SO<sub>2</sub> are  
 293 selected for the modeling study; the output variable  
 294 is  $F_{imp}$ . For a pure CO<sub>2</sub> stream,  $F_{imp}$  is equal to 1. The  
 295 value of  $F_{imp}$  for impure CO<sub>2</sub> is equal to the impure  
 296 CO<sub>2</sub> MMP divided by the pure CO<sub>2</sub> MMP of the same  
 297 oil. The data used for system training are from Alston  
 298 et al. (1985) and Dong (1999).

299 Various neural network architectures were investi-  
 300 gated to obtain desired models for predicting pure  
 301 CO<sub>2</sub> MMP and impure factor ( $F_{imp}$ ) as a function of  
 302 selected input variables. Different scenarios on the  
 303 number of hidden layers, the number of neurons in  
 304 each hidden layer, and the type of transfer function for  
 305 each neuron are analyzed. An architecture of one or  
 306 two hidden layers is initially used, followed by the  
 307 selections for the number of neurons and the types of  
 308 transfer functions (logic, sigmoid, or hyperbolic tan-

gent), with the target of obtaining the best fit to the  
 given data. 309 310

### 3. The training results 311

The scatter plots in Figs. 4–6 provide comparisons  
 of the measured CO<sub>2</sub> MMP levels with the ANN-  
 derived ones as well as those provided by Alston et al.  
 (1985) using statistical models. Figs. 4 and 5 present  
 312 313 314 315

t1.1 Table 1  
 t1.2 Statistical analysis for calibration results from the ANN and  
 statistical models (for MMP)

t1.3 Method	Average relative error (%)	Minimum relative error (%)	Maximum relative error (%)	Standard deviation (psia)	Correlation coefficient
t1.4 ANN (°F)	5.91	0.08	27.30	157.57	0.987
t1.5 ANN (K)	6.48	0.46	25.51	158.61	0.987
t1.6 Statistical	8.88	0.33	23.34	290.05	0.963

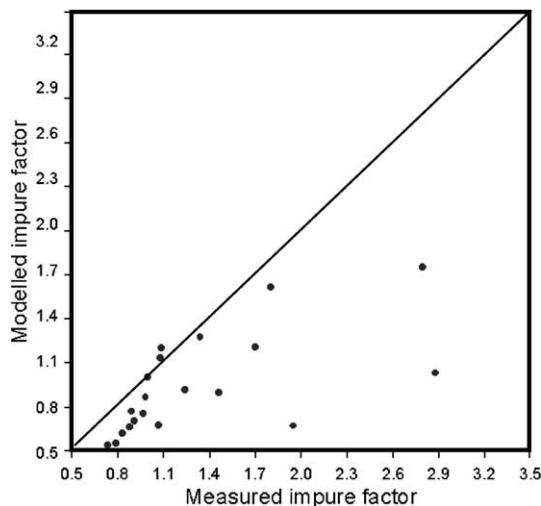


Fig. 8. The measured versus modeled impure factors (from Sebastian et al., 1984).

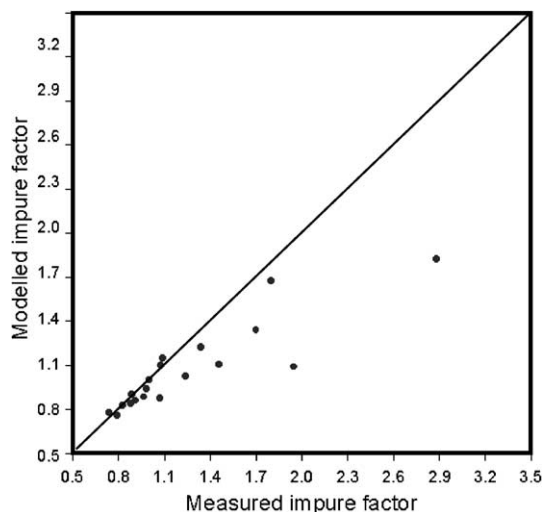


Fig. 9. The measured versus modeled impure factors (from Alston et al., 1985).

316 the error analysis of results with the input reservoir  
 317 temperatures expressed as Fahrenheit ( $^{\circ}\text{F}$ ) and Kelvin  
 318 (K), respectively. It is indicated that, when reservoir  
 319 temperature is expressed in different units ( $^{\circ}\text{F}$  and K),  
 320 the related ANN inputs will be different. These differ-  
 321 ent input data will then result in differences in training  
 322 and calibrating processes for the ANN model, leading  
 323 to varied relations between the measured and the  
 324 ANN-simulated MMP values. In this study, the two  
 325 sets of data were used to verify each other in order to  
 326 improve the model's performance. Fig. 6 shows the  
 327 error levels from the model of Alston et al. (1985)  
 328 based on the same data set but a different method  
 329 (statistical technique). As shown, the ANN models  
 330 produce much lower error levels, compared with the  
 331 statistical approach (Alston et al., 1985).

332 Table 1 shows the outputs of statistical analyses for  
 333 calibration results from the ANN and statistical mod-  
 334 els for MMP forecasting. It is indicated that the  
 335 developed ANN models have lower calibration errors

336 than those developed by Alston et al. (1985). In detail,  
 337 for the ANN model, the calibrated relative errors are  
 338 5.91% for  $^{\circ}\text{F}$  and 6.48% for K, and the correlation  
 339 coefficients are both 0.987. In comparison, for the  
 340 statistical model (Alston et al., 1985), the calibrated  
 341 relative error is 8.88%, and the correlation coefficient  
 342 is 0.963.

343 The scatter plots as shown in Figs. 7–9 provide  
 344 comparisons of the measured impure factor ( $F_{\text{imp}}$ )  
 345 values with the ANN-derived ones as well as those  
 346 provided by Sebastian et al. (1984) and Alston et al.  
 347 (1985) based on the same data set but different  
 348 statistical models. Much lower error levels were  
 349 encountered from the results of the ANN model,  
 350 compared with those of statistical approaches (Sebas-  
 351 tian et al., 1984; Alston et al., 1985). Table 2 shows  
 352 the outputs of statistical analyses for calibration  
 353 results from the ANN and statistical models for  
 354 impure factor ( $F_{\text{imp}}$ ) forecasting. It is indicated that  
 355 the developed ANN model has lower calibration  
 356 errors than those developed by Sebastian et al.  
 357 (1984) and Alston et al. (1985).

#### 4. Application to MMP and $F_{\text{imp}}$ forecasting 358

359 After the ANN models were established, they  
 360 could then be used for MMP and  $F_{\text{imp}}$  forecasting  
 361 under a variety of conditions. With measured data  
 362 sets that were not used for training, the modeling  
 363 outputs could then be compared with measured val-  
 364 ues to verify the model's accuracy. The data from  
 365 Rhuma (1992) were used to validate the accuracy of  
 366 ANN outputs for pure  $\text{CO}_2$  MMP. ANN verifications  
 367 for  $F_{\text{imp}}$  predictions were not conducted due to data  
 368 unavailability. The following applications of ANN for  
 369  $F_{\text{imp}}$  forecasting were based on an assumption that its  
 370 accuracy is comparable to that of MMP forecasting.

371 The predicted results of pure  $\text{CO}_2$  MMP are  
 372 showed in Figs. 10–12. Among them, Figs. 10

t2.1 Table 2  
 t2.2 Statistical analysis for calibration results from the ANN and statistical models (for impure factor)

t2.3 Method	Average relative error (%)	Minimum relative error (%)	Maximum relative error (%)	Standard deviation	Correlation coefficient
t2.4 ANN	3.83	0.12	8.87	0.07	0.99
t2.5 Statistical (Alston et al.)	13.25	0.16	44.14	0.45	0.80
t2.6 Statistical (Sebastian et al.)	25.25	0	65.68	0.62	0.63

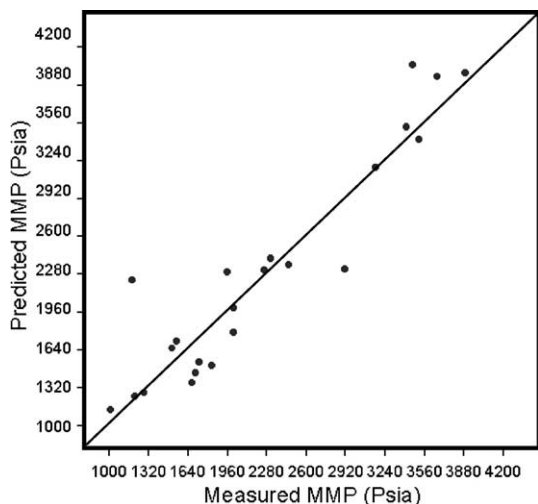


Fig. 10. The measured versus ANN-predicted MMP values (with °F for temperature).

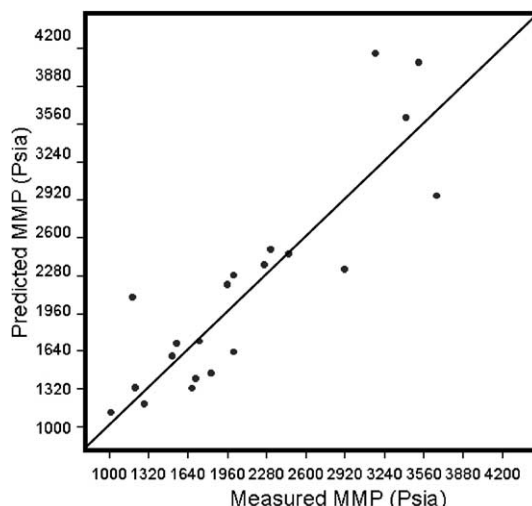


Fig. 12. The measured versus statistically predicted MMP values (from Alston et al., 1985).

373 and 11 are the prediction results of MMP obtained  
 374 from ANN models under different reservoir temper-  
 375 atures (°F and K); Fig. 12 shows the results from  
 376 Alston et al. (1985) using statistical methods. As  
 377 shown, higher prediction accuracies were obtained  
 378 by the ANN models, compared with those by statistical  
 379 approaches.

380 Table 3 shows the results of error analyses for  
 381 prediction outputs from the developed ANNs and the

statistical models of Alston et al. (1985). It is indicated  
 that outputs from the ANNs are more accurate than  
 those from the models of Alston et al. (1985). Com-  
 pared with the calibration results as shown in Table 1,  
 the relative errors and standard deviations become  
 higher, while the correlation coefficients are lower.  
 In detail, the average relative errors are 12.08% for °F  
 and 12.32% for K, and correlation coefficients are  
 0.936 for °F and 0.939 for K. However, the accuracy  
 and correlation level are still much higher than those of  
 statistical models (relative error=17.05%, and correla-  
 tion = 0.896).

With the developed ANNs models for MMP and  $F_{imp}$  forecasting, we can further study the variations of MMP under different reservoir temperatures,  $C_{5+}$  molecular weights, volatile oil fractions, and intermediate oil fractions. According to Alston et al. (1985), if the volatile oil fraction and intermediate oil fraction vary at the same rate, the MMP will remain constant. This is because the ratio of volatile oil fraction to intermediate

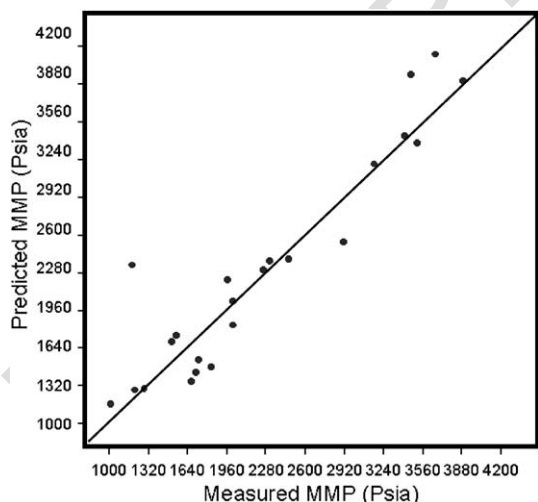


Fig. 11. The measured versus ANN-predicted MMP values (with K for temperature).

Method	Average relative error (%)	Minimum relative error (%)	Maximum relative error (%)	Standard deviation (psia)	Correlation coefficient
ANN (°F)	12.08	0.51	86.88	333.31	0.936
ANN (K)	12.32	0.09	96.83	337.32	0.939
Statistical	17.05	0.29	76.24	552.21	0.896



oil fraction is constant, even though the contents of solution gas are changing. In the real field, however, MMP will change even when the volatile oil fraction and the intermediate oil fraction vary at the same rate. In this study, the base points for the contents of solution gas are selected as  $X_{vol} = 16.09\%$  and  $X_{int} = 19.68\%$ . Thus, the contents of solution gas will then increase with increments of 2%, 4%, . . . , of the base points. In this way, the ratio of volatile oil fraction to intermediate oil fraction will keep to be a constant, while the contents of solution gas are changing dynamically. Using the developed ANN model, variations of MMP under given reservoir temperature and  $C_{5+}$  molecular weight but varying contents of solution gas can be examined.

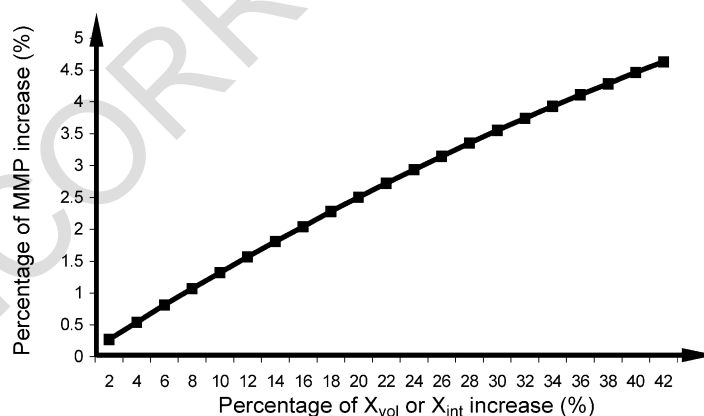
In general, MMP will be constant if effect of volatile-oil-fraction variation is the same as that of intermediate-oil-fraction variation. However, as shown in Fig. 13, MMP is an increasing function of the mole fractions of volatile oil and intermediate oil, even though  $X_{vol}/X_{int}$  is a constant. This indicates that the effect of  $X_{vol}$  variation is greater than that of  $X_{int}$  variation; conversely, if MMP was a decreasing function, the effect of  $X_{int}$  would be greater than that of  $X_{vol}$ . This result is consistent with the experimental results from Dong et al. (1999).

Through the developed ANN models, variations of  $CO_2$  MMP under different reservoir temperatures and  $C_{5+}$  molecular weights can be examined, with the

volatile oil fraction ( $X_{vol}$ ) and the intermediate oil fraction ( $X_{int}$ ) being fixed at 10.5% and 14.28%, respectively. Figs. 14 and 15 show that the MMPs increase with reservoir temperature and  $C_{5+}$  molecular weight. The relation between MMP and reservoir temperature is close to linear when the level of  $C_{5+}$  molecular weight is high. For many reservoir oils with nearly equal values of volatile and intermediate fractions, the developed ANNs can be used to quantify the relation between  $CO_2$  MMP and reservoir temperature under different  $C_{5+}$  molecular weights, such that forecasting of  $CO_2$  MMP becomes possible.

It is generally recognized that the effect of an impurity (or contaminant) on  $CO_2$  MMP depends on whether the impurity can enhance the  $CO_2$ 's solubility. This idea of the solubility was used to estimate the effects of impurities on  $CO_2$  MMP by Alston et al. (1985) and Sebastian et al. (1984), where they incorporated an average critical temperature of the gas mixture within the correlations. It was indicated that solvency could be improved if  $CO_2$  was diluted with an impurity whose critical temperature was higher than that of  $CO_2$ . However, the solvency deteriorated if  $CO_2$  was diluted with an impurity with a lower critical temperature. In general, the effects of  $H_2S$  and  $SO_2$  on MMP are less dramatic than those of  $CH_4$  and  $N_2$ .

Fig. 7 shows an excellent agreement between predicted and measured  $F_{imp}$  values. Thus, the



Note: (1) The base points of volatile and intermediate oil fractions are:  $X_{vol} = 16.09\%$  and  $X_{int} = 19.68\%$ ;

(2) The percentage of  $X_{vol}$  increase = the percentage of  $X_{int}$  increase.

Fig. 13. Variations of MMP with solution-gas contents (at  $T = 316$  K and  $M_{C_{5+}} = 196.1$ ).

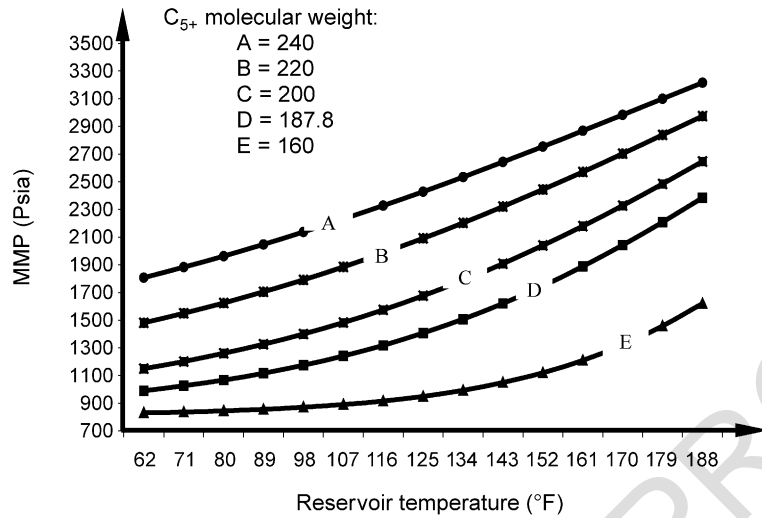


Fig. 14. Variations of MMP with temperature and C<sub>5+</sub> molecular weight (at X<sub>int</sub> = 10.5% and X<sub>vol</sub> = 14.28%) (with °F for temperature).

460 effects of each impurity (N<sub>2</sub>, C<sub>1</sub>, H<sub>2</sub>S or SO<sub>2</sub>) in the  
 461 CO<sub>2</sub> stream on the MMP can be examined by  
 462 simulating  $F_{imp}$  levels under different mole fractions  
 463 using the developed ANN model. The results are  
 464 shown in Fig. 16, indicating that N<sub>2</sub> has the most  
 465 significant effect; a small variation in N<sub>2</sub> content  
 466 could result in a great fluctuation in CO<sub>2</sub> MMP  
 467 level. The content of C<sub>1</sub> is also an increasing  
 468 function of CO<sub>2</sub> MMP level, with a less significant  
 469 effect. In comparison, the contents of H<sub>2</sub>S and SO<sub>2</sub>

are slightly decreasing functions of MMP. There- 470  
 fore, N<sub>2</sub> is the most important impurity which 471  
 should be well considered before the recycled CO<sub>2</sub> 472  
 is reinjected. 473

In Fig. 16, MMP is an increasing function of N<sub>2</sub> 474  
 concentration. The MMP increases rapidly when the 475  
 N<sub>2</sub> concentration is between 4% and 9%. Thus, keep- 476  
 ing N<sub>2</sub> concentration lower than 4% would be a 477  
 desired strategy. Attempts to reduce N<sub>2</sub> concentration 478  
 to lower than 4% could lead to low efficiencies and 479

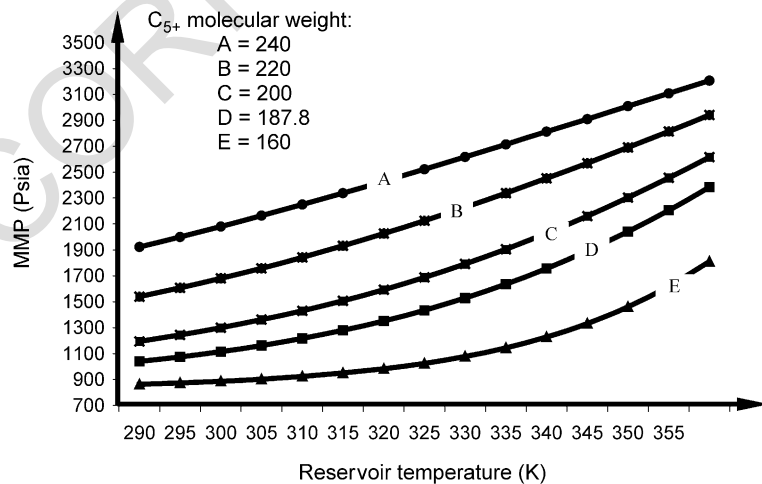


Fig. 15. Variations of MMP with temperature and C<sub>5+</sub> molecular weight (at X<sub>int</sub> = 10.5% and X<sub>vol</sub> = 14.28%) (with K for temperature).

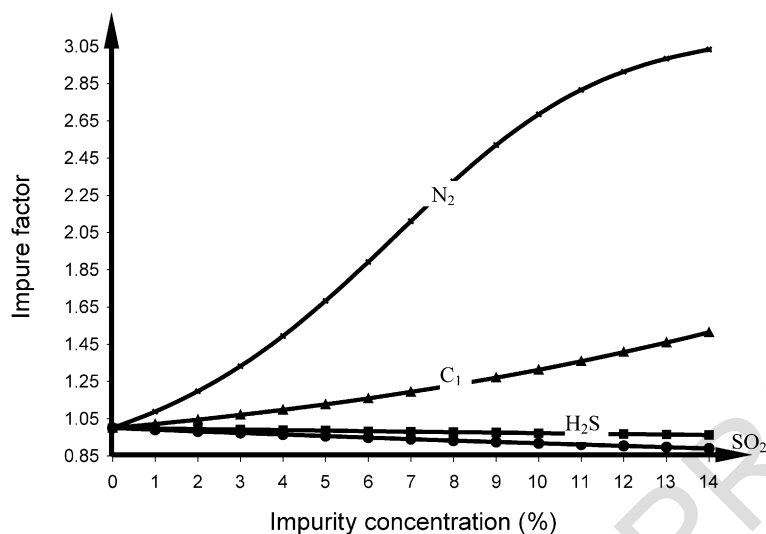


Fig. 16. The predicted values of impure factor as functions of impurity concentrations.

480 high costs. This information is important for deter-  
 481 mining the desired removal rate of N<sub>2</sub> in the recycled  
 482 CO<sub>2</sub> stream.

## 483 5. Discussion

484 Conventional pressure, volume and temperature  
 485 (PVT) simulation techniques can directly address  
 486 complexities associated with factors that affect the  
 487 MMP level. However, such simulation efforts often  
 488 suffer from problems of data unavailability for specify-  
 489 ing complicated state equations and quantifying inter-  
 490 relationships among various system components. This  
 491 might lead to over simplification of the related pro-  
 492 cesses and thus reduced prediction accuracy. On the  
 493 other hand, although statistical models have lower  
 494 requirements in terms of data availability, the associ-  
 495 ated difficulties in satisfying many rigid assumptions  
 496 that are essential for justifying their applications have  
 497 affected their performances.

498 In this study, the ANN approach is for the first time  
 499 used to predict MMP and  $F_{imp}$ . The results demon-  
 500 strate that, under conditions with limited field infor-  
 501 mation, the ANN approach could produce a higher  
 502 accuracy than statistical models.

503 Prediction of CO<sub>2</sub> MMP is critical for CO<sub>2</sub>  
 504 flooding in enhanced oil recovery processes. An

inaccurate prediction may result in significant con- 505  
 sequences. For example, recommendation for a too 506  
 high operating level of MMP may result in greatly 507  
 inflated operation costs as well as occupational 508  
 health concerns. On the other hand, if the suggested 509  
 MMP is too low, the miscible displacement process 510  
 would become ineffective, leading to a high risk of 511  
 system failure. Thus, a higher prediction accuracy 512  
 would bring significant economic benefits. 513

In the last few years, more and more attentions 514  
 have been paid on the use of recycled CO<sub>2</sub> for 515  
 enhanced oil recovery, because of the worldwide 516  
 concern on the issue of greenhouse gas emissions. 517  
 In the recycled CO<sub>2</sub> stream, however, a variety of 518  
 impurities exist and may significantly affect the 519  
 MMP. At the same time, it is costly to purify the 520  
 CO<sub>2</sub> stream. Therefore, identification of a suitable 521  
 level of impurity removal rate (and thus a suitable 522  
 level of impurity contents in the CO<sub>2</sub> stream which 523  
 can be tolerated for miscible injections) is desired. 524  
 The developed ANN model for  $F_{imp}$  forecasting can 525  
 supply such information in terms of the relations 526  
 between  $F_{imp}$  levels and impurity contents in the 527  
 CO<sub>2</sub> stream, and thus help to identify an optimum 528  
 removal rate. Thus, the chance of economic losses 529  
 due to either unnecessarily too high removal rate (and 530  
 thus an increased operating costs) or too low rate (and 531  
 thus a raised risk of inflated MMP) can be minimized. 532

533 **6. Conclusions**

534 In this study, ANN models for predicting CO<sub>2</sub>  
 535 minimum miscibility pressures (MMP) and impure  
 536 CO<sub>2</sub> MMP factor ( $F_{imp}$ ) have been developed. The  
 537 interrelations of CO<sub>2</sub> MMPs with molecular weight of  
 538 C<sub>5+</sub> fraction, reservoir temperature, volatile oil frac-  
 539 tion, and intermediate oil fraction have been analyzed,  
 540 resulting in a trained ANN model. Moreover, corre-  
 541 lations between the impure CO<sub>2</sub> MMP factor ( $F_{imp}$ )  
 542 and the contaminant concentrations in the CO<sub>2</sub> stream  
 543 have been examined. The developed ANN models  
 544 have been used then to predict the variations of CO<sub>2</sub>  
 545 MMP with MW of C<sub>5+</sub> fraction, temperature of  
 546 reservoir, and contaminant contents in CO<sub>2</sub> stream.  
 547 The effectiveness of the developed ANN models was  
 548 also evaluated by comparing its prediction results with  
 549 measured MMP levels and prediction results from  
 550 other statistical models. The modeling results indicate  
 551 that reasonable predictions have been generated.  
 552 Especially, under conditions with limited field infor-  
 553 mation, the ANN approach could produce a higher  
 554 accuracy than statistical models.

555 In this study, the ANN approach is for the first time  
 556 used to predict MMP and  $F_{imp}$ . With the increased  
 557 prediction accuracy, the developed models can help to  
 558 identify the desired operating levels of MMP and the  
 559 suitable levels of impurity removal rates in enhanced  
 560 oil recovery processes. Pool operators can thus opti-  
 561 mize the injection gas to improve the process eco-  
 562 nomics. This provision of effective decision support  
 563 would bring tremendous economic efficiencies for oil  
 564 industries. In practical applications of the model,  
 565 continuous updates of the modeling system are rec-  
 566 ommended as long as new field operation data  
 567 become available. The developed ANN models are  
 568 user-friendly and can be easily utilized by engineers in  
 569 petroleum industry.

570 The ANN method has been utilized in a number of  
 571 applications in petroleum industry. This study is an  
 572 extension of the previous efforts. It is the first attempt  
 573 in using ANN to facilitate forecasting of CO<sub>2</sub> mini-  
 574 mum miscibility pressures (MMP) and impure CO<sub>2</sub>  
 575 MMP factors. When applying the ANN to this new  
 576 area, a number of innovative considerations need to be  
 577 made to effectively reflect the effects of many impact  
 578 factors and their interactions. For example, the inter-  
 579 relations of CO<sub>2</sub> MMPs with molecular weight of C<sub>5+</sub>

fraction, reservoir temperature, volatile oil fraction, 580  
 and intermediate oil fraction, as well as the correla- 581  
 tions between the impure CO<sub>2</sub> MMP factor and the 582  
 contaminant concentrations in the CO<sub>2</sub> stream, have 583  
 been examined through the developed ANN frame- 584  
 work. These interrelationships could hardly be 585  
 addressed through traditional approaches, while the 586  
 ANN approach shows advantages in reflecting such 587  
 complex uncertainty and nonlinearity. 588

589 **7. Uncited references**

Ahmed, 1992 590

Lake, 1989 591

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595 **References**

- Ahmed, N.R., 1992. Minimum Miscibility Pressures of CO<sub>2</sub>/Hydro- 596  
 carbon Systems; Evaluation of Existing Prediction Methods and 597  
 Development of a New Correlation. MSc Thesis, University of 598  
 Saskatchewan. 599
- Alston, R.B., Kokolis, G.P., James, C.F., 1985. CO<sub>2</sub> minimum mis- 600  
 miscibility pressures: a correlation for impure CO<sub>2</sub> streams and live 601  
 oil systems. SPE J., 268–274 (April). 602
- Cardenas, R.L., et al., 1984. Laboratory design of a gravity-stable, 603  
 miscible CO<sub>2</sub> process. J. Pet. Technol., 111–118 (Jan.). 604
- Cronquist, C., 1978. Carbon dioxide dynamic miscibility with light 605  
 reservoir oils. Proc. Fourth Annual U.S. DOE Symposium, Tulsa, 606  
 vol. 1B-oil, pp. 28–30 (Aug.). 607
- Dayhoff, J.E., 1990. Neural Network Architectures, Van Nostrand- 608  
 Reinhold, New York. 609
- Dicharry, R.M., Peryman, T.L., Ronquille, J.D., 1973. Evaluation 610  
 and design of a CO<sub>2</sub> miscible flood project-SACROC unit, 611  
 Kelly–Snyder field. J. Pet. Technol., 1309–1318 (Nov.). 612
- Dong, M., 1999. Task 3—minimum miscibility pressure (MMP) 613  
 studies, in the Technical Report: Potential of Greenhouse Stor- 614  
 age and Utilization through Enhanced Oil Recovery. Petroleum 615  
 Technology Research Centre, Saskatchewan Research Council 616  
 (SRC Publication No. P-110-468-C-99), September. 617
- Dong, M., Huang, S., Srivastava, R., 2000. Effect of solution gas in 618  
 oil on CO<sub>2</sub> minimum miscibility pressure. J. Can. Pet. Technol. 619  
 39 (11), 53–61. 620
- Dunyushkin, I.I., Namiot, A.Y., 1979. Mixing conditions of oil with 621  
 carbon dioxide. Neft Khozvaistvo (Mar.). 622

- 623 Gardner, J.W., Orr, F.M., Patel, P.D., 1981. The effect of phase  
624 behavior on CO<sub>2</sub> flood displacement efficiency. *J. Pet. Technol.*,  
625 2067–2081 (Nov.).
- 626 Frimodig, J.P., Reese, N.A., Williams, C.A., 1983. Carbon dioxide  
627 flooding evaluation of high-pour-point, paraffinic red wash reser-  
628 voir oil. *Soc. Pet. Eng. J.*, 587–594 (Aug.).
- 629 Gharbi, R.B., Elsharkawy, A.M., 1996. Neural network model for  
630 estimating the PVT properties of Middle East crude oils. *In Situ*  
631 20 (4), 367–394.
- 632 Gharbi, R.B., Elsharkawy, A.M., 1999. Neural network model for  
633 estimating the PVT properties of Middle East crude oils. *SPE*  
634 *Reserv. Evalu. Eng.* 2 (3), 255–265 (June).
- 635 Graue, D.J., Zana, E.T., 1981. Study of a possible CO<sub>2</sub> flood in  
636 rangely field. *J. Pet. Technol.*, 1312–1318 (July).
- 637 Grigg, R.B., Schechter, D.S., 1997. State of the industry in CO<sub>2</sub>  
638 floods. SPE Paper 38849 Presented at the 1997 SPE Annual  
639 Technical Conference and Exhibition held in San Antonio,  
640 Texas, October 5–8.
- 641 Jacobson, H.A., 1972. Acid gases and their contribution to misci-  
642 bility. *J. Can. Pet. Technol.*, 56–59 (April–June).
- 643 Johnson, J.P., Pollin, J.S., 1981. Measurement and correlation of  
644 CO<sub>2</sub> miscibility pressures. Paper SPE 9790 Presented at the  
645 1981 SPE/DOE Enhanced Oil Recovery Symposium, Tulsa,  
646 April 5–8.
- 647 Kovarik, F.S., 1985. A minimum miscibility pressure study using  
648 impure CO<sub>2</sub> and West Texas oil systems: data base, correlations  
649 and compositional simulation. Paper SPE 14689 Presented at the  
1985 SPE Production Technology Symposium, Lubbock, Nov. 650  
11–12. 651
- Lake, L.W., 1989. *Enhanced Oil Recovery*. Prentice-Hall, New 652  
Jersey. 653
- Mungan, N., 1981. Carbon dioxide flooding-fundamentals. *J. Can.* 654  
*Pet. Technol.*, 87–92 (Jan.). 655
- Sebastian, H.M., Wenger, R.S., Renner, T.A., 1984. Correlation of  
656 minimum miscibility pressure for impure CO<sub>2</sub> streams. Paper  
657 SPE 12648 Presented at the 1984 SPE/DOE Enhanced Oil Re-  
658 covery Symposium, Tulsa, April 15–18. *JPT* (1985), 37 (2),  
659 268–274. 660
- Waller, M.D., Rowsell, P.J., 1994. Intelligent well control. *Trans.* 661  
*Inst. Min. Metall.* 103, 47–51. 662
- White, T.M., Lindsay, R.F., 1972. Enhanced oil recovery by CO<sub>2</sub>  
663 miscible displacement in the Little Knife Field, Billings County,  
664 North Dakota. *Proc., 5th Annual DOE Symposium on Enhanced*  
665 *Oil and Gas Recovery and Improved Drilling Technology*, Tulsa  
666 2-Oil, N-5. 667
- Wittstrom Jr., M.D., Hagemeyer, M.E., 1978. A review of Little  
668 Knife Field development, North Dakota. *Proc., Williston Basin*  
669 *Symposium*. Montana Geological Society, pp. 361–368. 670
- Yellig, W.F., Metcalfe, R.S., 1980. Determination and prediction of  
671 CO<sub>2</sub> minimum miscibility pressures. *J. Pet. Technol.*, 160–168  
672 (Jan.). 673
- Zuo, Y.X., Chu, J.Z., Ke, S.L., Guo, T.M., 1993. A study of the  
674 minimum miscibility pressure for miscible flooding systems. *J.*  
675 *Pet. Sci. Eng.* 8, 315–328. 676