

**Math 415 - Applied Linear Algebra**  
**Fall 2010, section D1**  
**Exam 2 review sheet**

Here are the types of questions you should be able to answer and explain on exam 2.

- Is  $S$  a subspace of  $V$ ?
- Is  $v$  in  $\text{Span}\{v_1, \dots, v_k\}$ ? If so, express it as a linear combination of  $v_1, \dots, v_k$ .
- Do the vectors  $v_1, \dots, v_k$  span  $V$ ?
- Are  $v_1, \dots, v_k$  linearly independent? If not, find a dependence relation among them.
- Find a basis of  $\text{Span}\{v_1, \dots, v_k\}$  (and in particular its dimension).
- Find the transition matrix from one basis to another, and find the coordinates of a vector in different bases.
- Describe the solution(s) of the system  $Ax = b$  knowing the rank of  $A$ .
- Is  $L: V \rightarrow W$  a linear transformation?
- Find the standard matrix representation of  $L: \mathbb{R}^n \rightarrow \mathbb{R}^m$ .
- Find bases of  $\ker(L)$  and  $\text{im}(L)$ .
- Find the matrix representation of  $L: V \rightarrow W$  relative to bases  $\{v_1, \dots, v_n\}$  of  $V$  and  $\{w_1, \dots, w_m\}$  of  $W$ .