1. Chain Rule:

- (a) Let $h(t) = \sin(\cos(\tan t))$. Find the derivative with respect to t.
- (b) Let $s(x) = \sqrt[4]{x}$ where $x(t) = \ln(f(t))$ and f(t) is a differentiable function. Find $\frac{ds}{dt}$.

2. Parametrized curves:

(a) Describe and sketch the curve given parametrically by

$$\begin{cases} x = 5\sin(3t) \\ y = 3\cos(3t) \end{cases} \quad \text{for} \quad 0 \le t < \frac{2\pi}{3}.$$

What happens if we instead allow t to vary between 0 and 2π ?

- (b) Set up, but **do not evaluate** an integral that calculates the arc length of the curve described in part (a).
- (c) Consider the equation $x^2 + y^2 = 16$. Graph the set of solutions of this equation in \mathbb{R}^2 and find a parametrization that traverses the curve once counterclockwise.

3. 1st and 2nd Derivative Tests:

- (a) Use the 2nd Derivative Test to classify the critical numbers of the function $f(x) = x^4 8x^2 + 10$.
- (b) Use the 1st Derivative Test and find the extrema of $h(s) = s^4 + 4s^3 1$.
- (c) Explain why the 2nd Derivative test is unable to classify all the critical numbers of $h(s) = s^4 + 4s^3 1$.

4. Consider the function $f(x) = x^2 e^{-x}$.

- (a) Find the best linear approximation to f at x = 0.
- (b) Compute the second-order Taylor polynomial at x = 0.
- (c) Explain how the second-order Taylor polynomial at x = 0 demonstrates that f must have a local minimum at x = 0.

5. Consider the integral $\int_0^{\sqrt{3\pi}} 2x \cos(x^2) dx$.

- (a) Sketch the area in the *xy*-plane that is implicitly defined by this integral.
- (b) To evaluate, you will need to perform a substitution. Choose a proper u = f(x) and rewrite the integral in terms of u. Sketch the area in the uv-plane that is implicitly defined by this integral.
- (c) Evaluate the integral $\int_0^{\sqrt{3\pi}} 2x \cos(x^2) dx$.